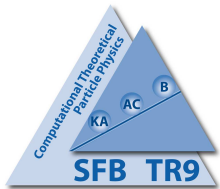


# QCD CORRECTIONS IN VBFNLO

Dieter Zeppenfeld  
Karlsruhe Institute of Technology



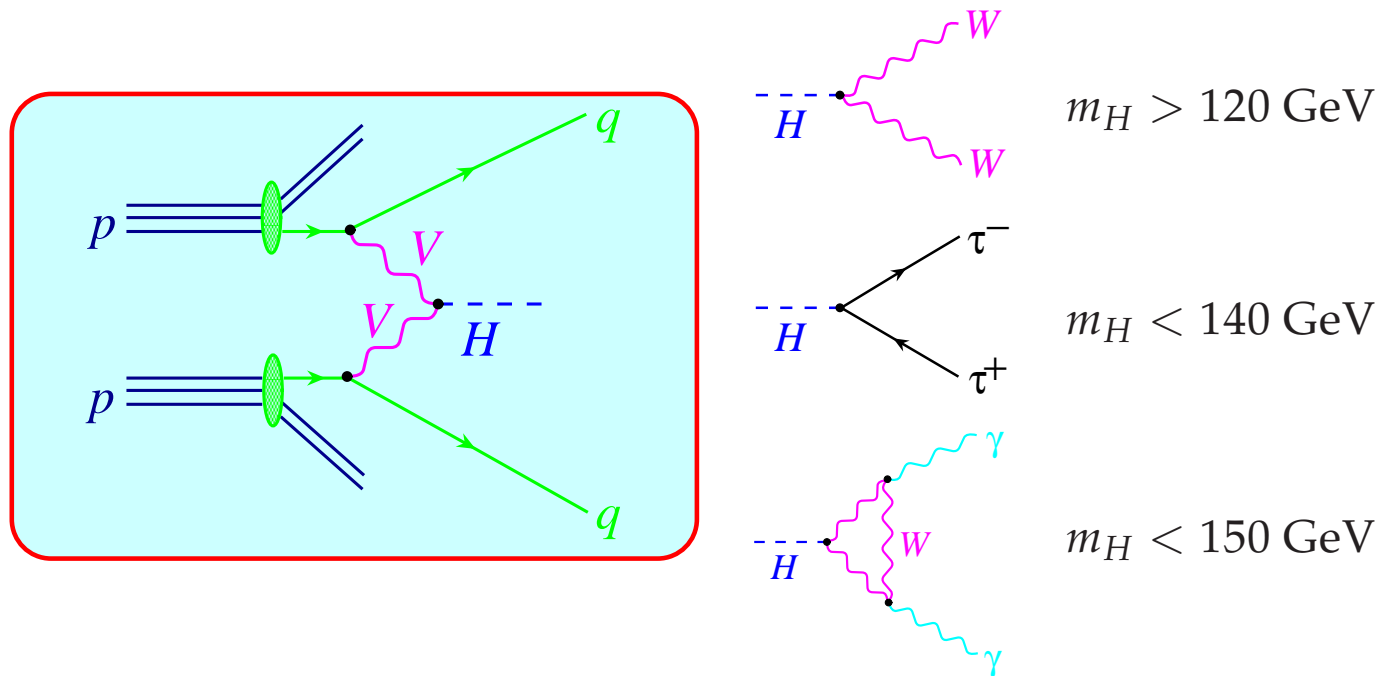
Mini-Workshop on PDFs and Standard Candles at the LHC  
Karlsruhe, March 19, 2012



Bundesministerium  
für Bildung  
und Forschung

- Vector Boson Fusion
- NLO QCD corrections to VV scattering
- Other NLO QCD processes in VBFNLO
- Conclusions

## Vector Boson Fusion

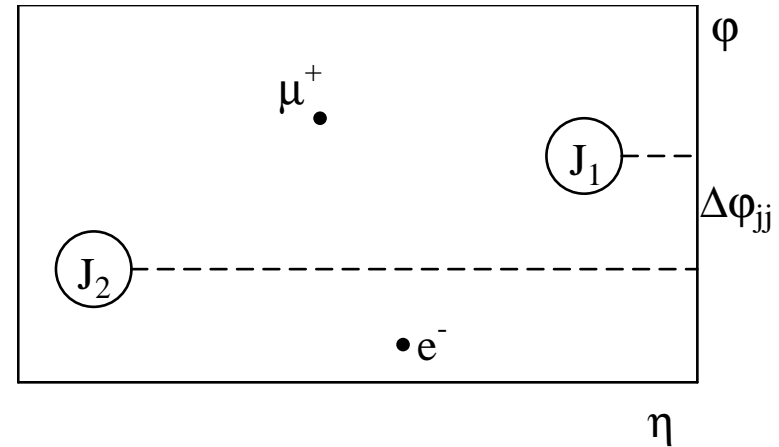
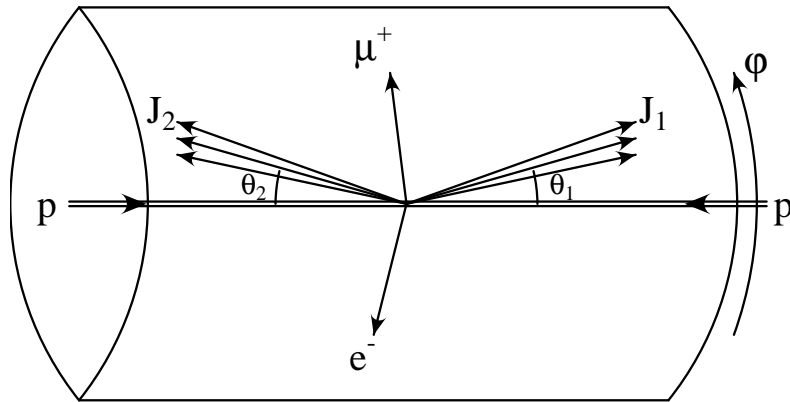


[Eboli, Hagiwara, Kauer, Plehn, Rainwater, D.Z. ...]

Most measurements can be performed at the LHC with **statistical accuracies** on the measured cross sections times decay branching ratios,  $\sigma \times \text{BR}$ , of **order 10%**.

**Would like theory errors below 5%  $\implies$  Need NLO corrections**

## VBF signature



### Characteristics:

- energetic jets in the **forward** and **backward** directions ( $p_T > 20$  GeV)
- large **rapidity separation** and large **invariant mass** of the two tagging jets
- **Higgs decay products between** tagging jets
- Little gluon radiation in the central-rapidity region, due to **colorless** W/Z exchange (**central jet veto**: no extra jets between tagging jets)

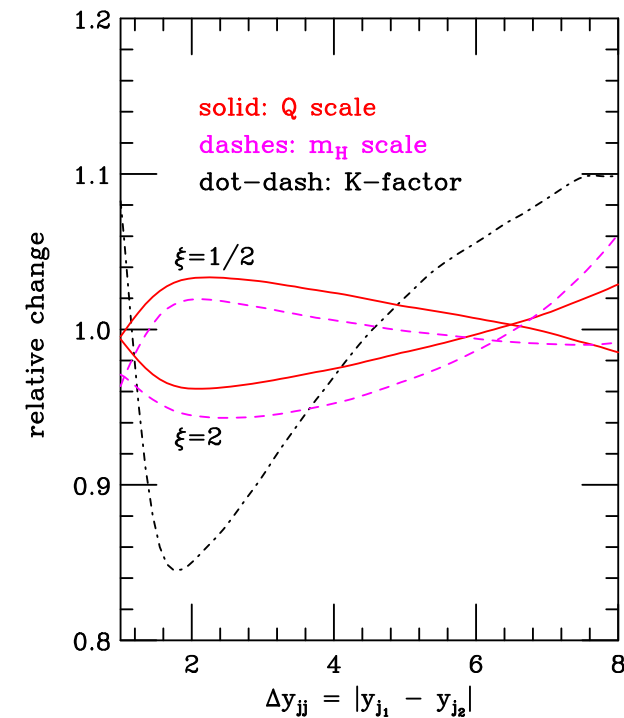
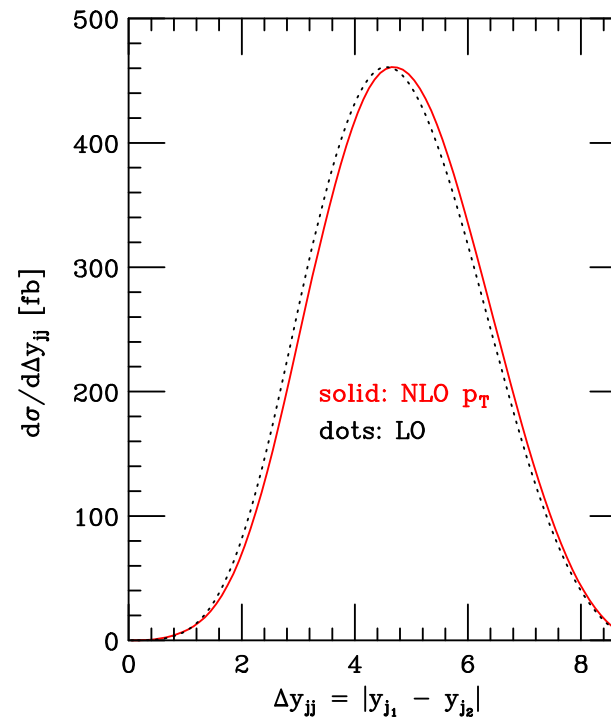
# NLO QCD corrections to VBF

- Small QCD corrections of  $\mathcal{O}(10\%)$
- Tiny scale dependence at NLO
  - $\pm 5\%$  for distributions
  - $< 2\%$  for  $\sigma_{\text{total}}$
- K-factor is phase space dependent
- QCD corrections under excellent control confirmed by NNLO corrections to inclusive VBF cross section  
 Bolzoni, Maltoni, Moch, Zaro  
 arXiv:1003.4451

✗ Need electroweak corrections for 5% uncertainty

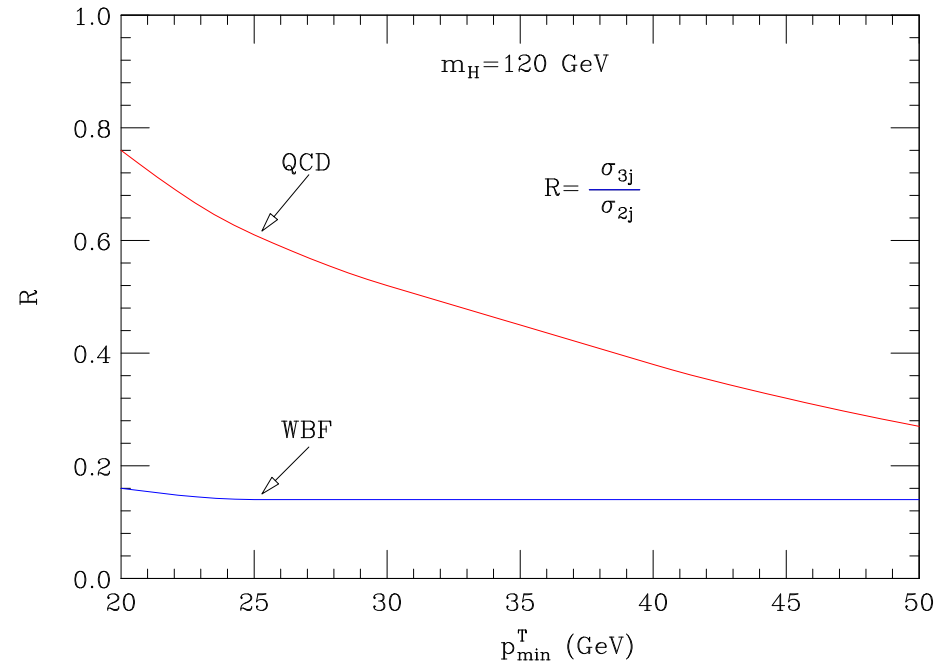
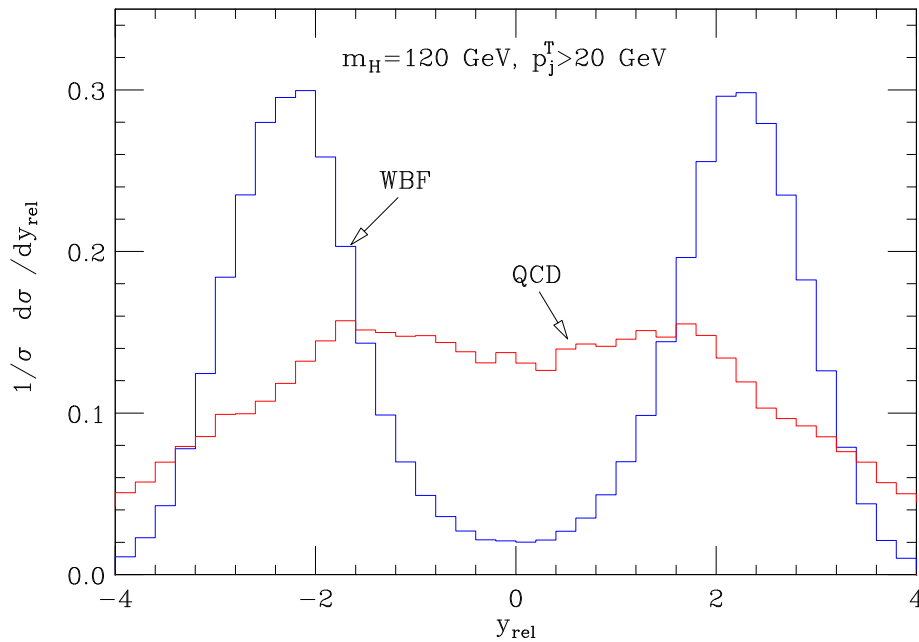
Ciccolini, Denner, Dittmaier, 0710.4749

Figy, Palmer, Weiglein arXiv:1012.4789



$m_H = 120 \text{ GeV}$ , typical VBF cuts

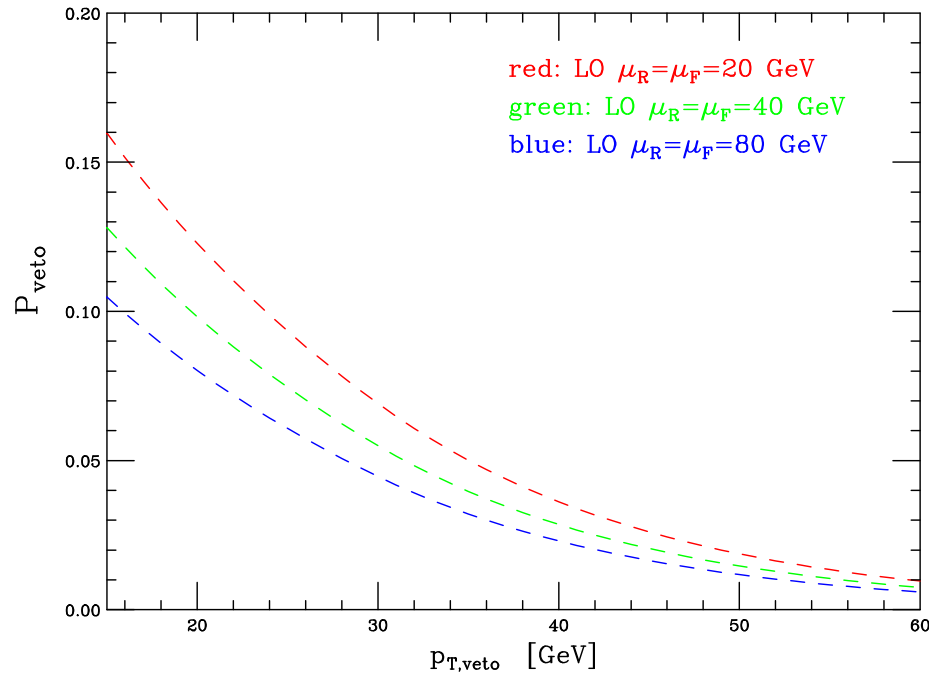
## Central Jet Veto: $Hjjj$ from VBF vs. gluon fusion



[ Del Duca, Frizzo, Maltoni, JHEP 05 (2004) 064]

- Angular distribution of third (softest) jet follows classically expected radiation pattern
- QCD events have higher effective scale and thus produce harder radiation than VBF (larger three jet to two jet ratio for QCD events)
- Central jet veto can be used to distinguish Higgs production via GF from VBF

## VBF Higgs signal and CJV



$$p_{Tj}^{veto} > p_{T,veto}, \quad \eta_j^{veto} \in (\eta_j^{\text{tag } 1}, \eta_j^{\text{tag } 2})$$

$$P_{\text{veto}} = \frac{1}{\sigma_2^{\text{NLO}}} \int_{p_{T,veto}}^{\infty} dp_{Tj}^{veto} \frac{d\sigma_3^{\text{LO}}}{dp_{Tj}^{veto}}$$

- Scale variation at LO for  $\sigma_{3j}$ :  $+33\%$  to  $-17\%$  for  $p_{T,veto} = 15$  GeV
- The uncertainty in  $P_{\text{veto}}$  feeds into the uncertainty of coupling measurements at the LHC
- In order to constrain couplings more precisely, the **NLO QCD corrections to  $Hjjj$**  are needed:  
T. Figy, V. Hankele, and DZ, arXiv:0710.5621 (JHEP)

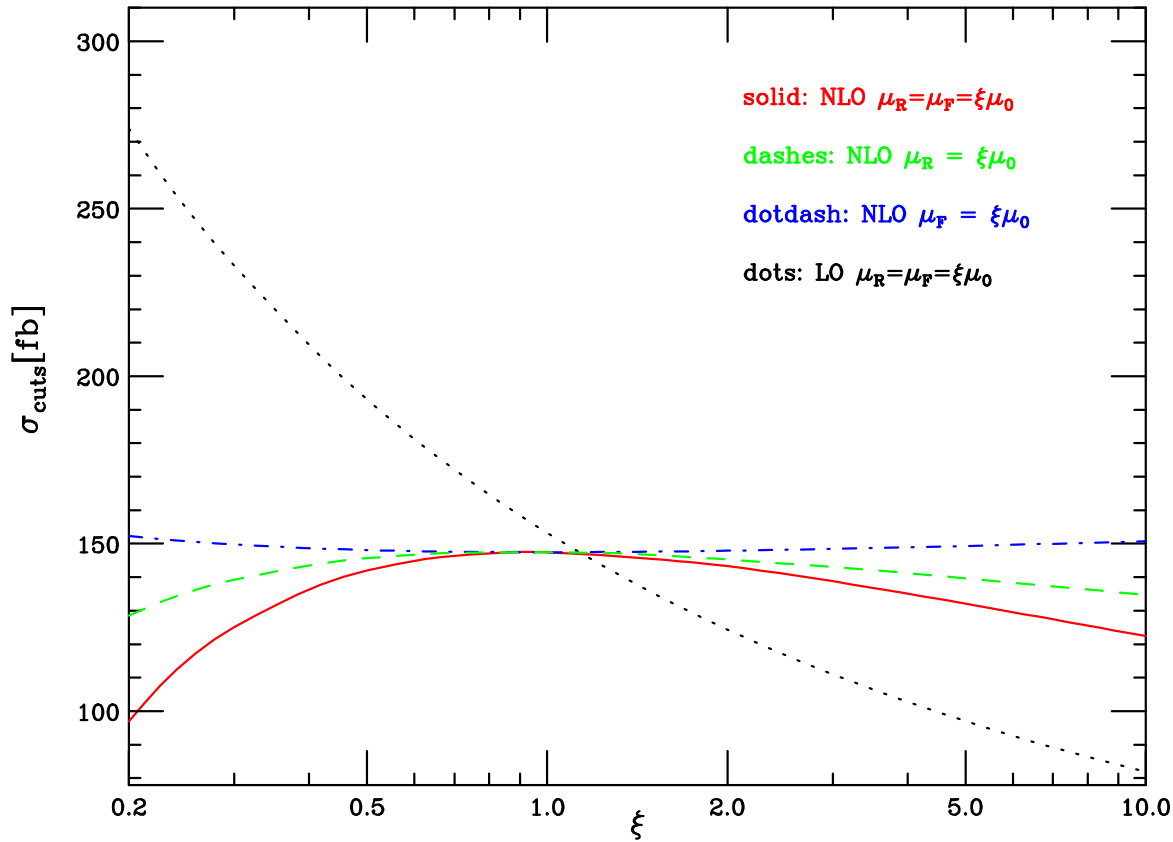
## Ingredients of the NLO Calculation

- Born: 3 final state partons + Higgs via VBF

$$\mathcal{M}_B = \delta_{i_2 i_b} t_{i_1 i_a}^{a_3} \left[ \begin{array}{c} \mathcal{M}_{B,1a} : \\ \begin{array}{cc} \begin{array}{c} 3 \\ \text{---} \\ a \end{array} \begin{array}{c} \text{---} \\ \text{---} \\ b \end{array} \\ \begin{array}{c} \text{---} \\ \text{---} \\ 1 \\ \text{---} \\ \text{---} \\ 2 \end{array} \\ \begin{array}{c} \text{---} \\ \text{---} \\ H \end{array} \end{array} & \begin{array}{cc} \begin{array}{c} 3 \\ \text{---} \\ a \end{array} \begin{array}{c} \text{---} \\ \text{---} \\ b \end{array} \\ \begin{array}{c} \text{---} \\ \text{---} \\ 1 \\ \text{---} \\ \text{---} \\ 2 \end{array} \\ \begin{array}{c} \text{---} \\ \text{---} \\ H \end{array} \end{array} \end{array} \right] \\
 + \delta_{i_1 i_a} t_{i_2 i_b}^{a_3} \left[ \begin{array}{c} \mathcal{M}_{B,2b} : \\ \begin{array}{cc} \begin{array}{c} a \end{array} \begin{array}{c} \text{---} \\ \text{---} \\ b \end{array} \\ \begin{array}{c} \text{---} \\ \text{---} \\ 1 \\ \text{---} \\ \text{---} \\ 2 \end{array} \\ \begin{array}{c} \text{---} \\ \text{---} \\ H \end{array} \end{array} & \begin{array}{cc} \begin{array}{c} a \end{array} \begin{array}{c} \text{---} \\ \text{---} \\ b \end{array} \\ \begin{array}{c} \text{---} \\ \text{---} \\ 1 \\ \text{---} \\ \text{---} \\ 2 \end{array} \\ \begin{array}{c} \text{---} \\ \text{---} \\ H \end{array} \end{array} \end{array} \right]$$

- Catani, Seymour subtraction method
- Real: 4 final state partons + Higgs via VBF
- Virtual: Two classes of gauge invariant subsets
  - Box + Vertex + Propagator
  - Pentagon + Hexagon **are small and can be neglected**

# Total $Hjjj$ Cross Section at the LHC: NLO vs LO

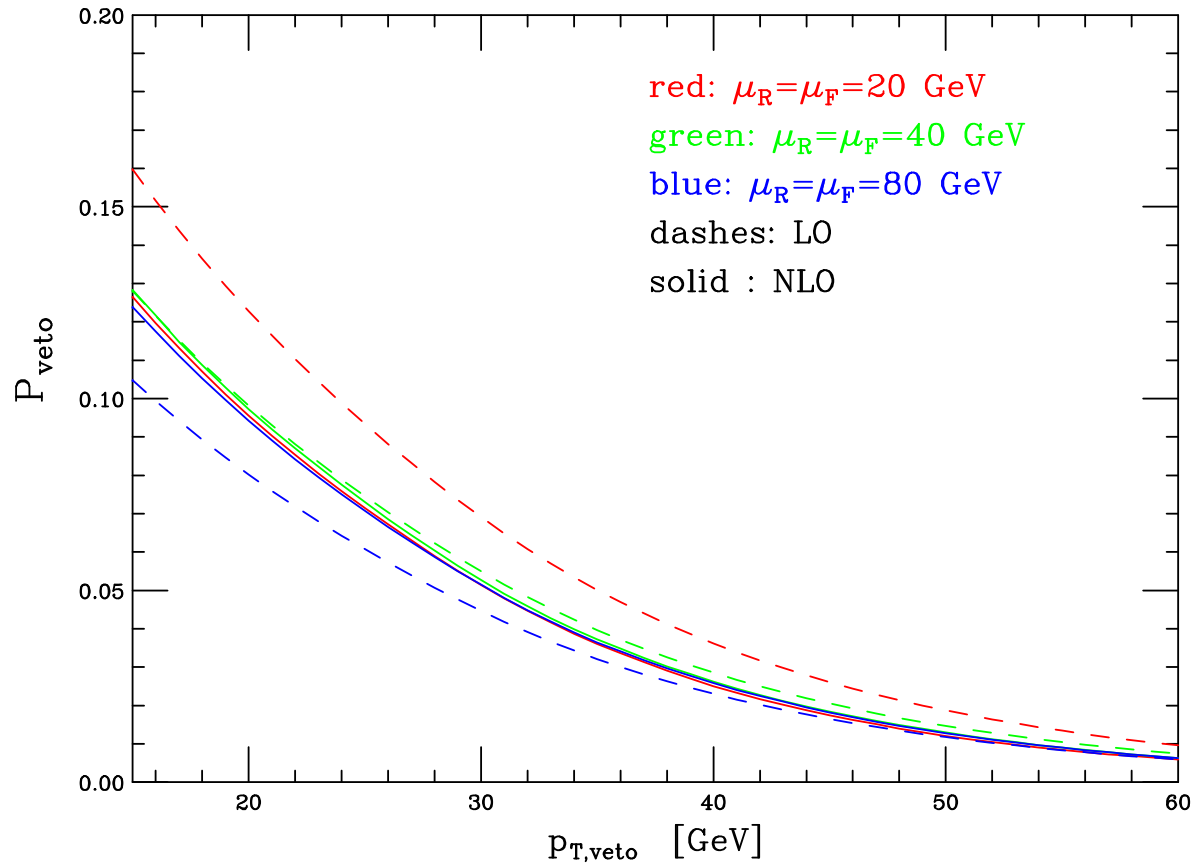


$\mu_0 = 40 \text{ GeV}$   
 $\xi = 2^{\mp 1}$  scale variations:

- LO: +26% to -19%
- NLO: less than 5%



## Veto Probability for the VBF Signal



$$P_{\text{veto}} = \frac{1}{\sigma_2^{\text{NLO}}} \int_{p_{T,\text{veto}}}^{\infty} dp_{Tj}^{\text{veto}} \frac{d\sigma_3}{dp_{Tj}^{\text{veto}}}$$

Scale variations,  $p_{T,\text{veto}} = 15$  GeV:

- LO: +33% to -17%
- NLO: -1.4% to -3.4%

Reliable prediction for **perturbative** part of veto probability at NLO

## NLO corrections available in VBFNLO

Parton level Monte Carlo programs for various NLO calculations, including

- QCD corrections for Higgs production via VBF

Figy, Oleari, DZ

Now includes electroweak and SUSY corrections to VBF Higgs production

Figy, Palmer, Weiglein

- QCD corrections to Higgs plus 3 jet production in VBF

Figy, Hankele, DZ

- QCD corrections to VBF  $W$  and  $Z$  production ( $qq \rightarrow qqV$ )

Oleari, DZ

- QCD corrections to weak boson scattering processes ( $qq \rightarrow qqVV$ )

Jäger, Oleari, DZ

Code is available at <http://www-itp.particle.uni-karlsruhe.de/~vbfnlweb/>

## Limitations of the $qq \rightarrow qqH$ picture

At  $m_H >$  few hundred GeV (for say  $\Gamma_H/m_H > 0.1$ ) we need to take interference with continuum electroweak into account

### Implication:

- Consider full processes  $qq \rightarrow qqVV$  or  $qq \rightarrow qq\bar{f}_1 f_2 \bar{f}_3 f_4$
- s-channel Higgs exchange graph with inverse propagator

$$\Delta_H(s) = s - s_H = s - m_H^2 + im_H\Gamma_H$$

is just one contribution.

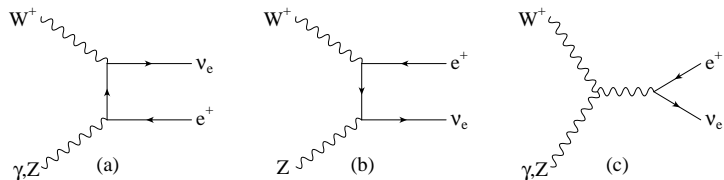
**Note:**  $m_H$  and  $\Gamma_H$  should be treated as free parameters for heavy Higgs

( $\Gamma_H$  should not necessarily be calculated in SM because EW precision tests give  $m_H < 152$  GeV: for larger  $m_H$  **there must be BSM effects** which should also affect the relation between  $m_H$  and  $\Gamma_H$  as well as  $HVV$  couplings)

# Weak boson scattering: $qq \rightarrow qqWW, qqZZ, qqWZ$ at NLO

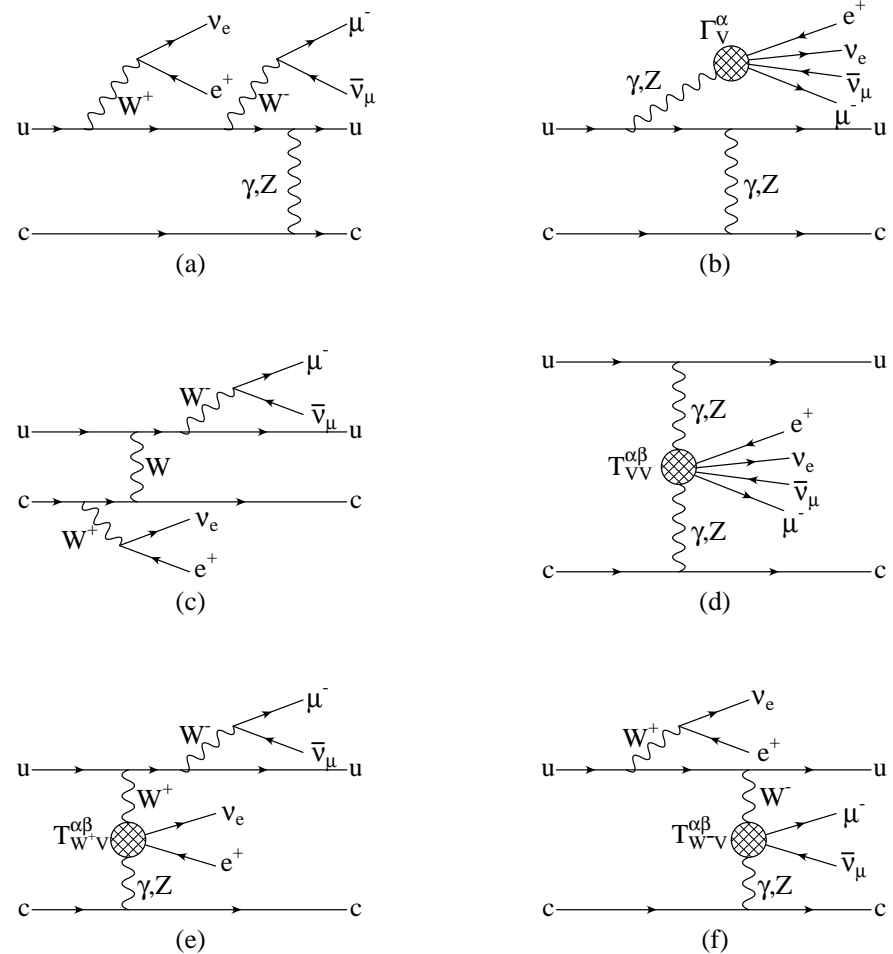
- example: WW production via VBF with leptonic decays:  $pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu + 2j$
- Spin correlations of the final state leptons
- All resonant and non-resonant Feynman diagrams included
- NC  $\implies$  181 Feynman diagrams at LO
- CC  $\implies$  92 Feynman diagrams at LO

Use modular structure, e.g. leptonic tensor



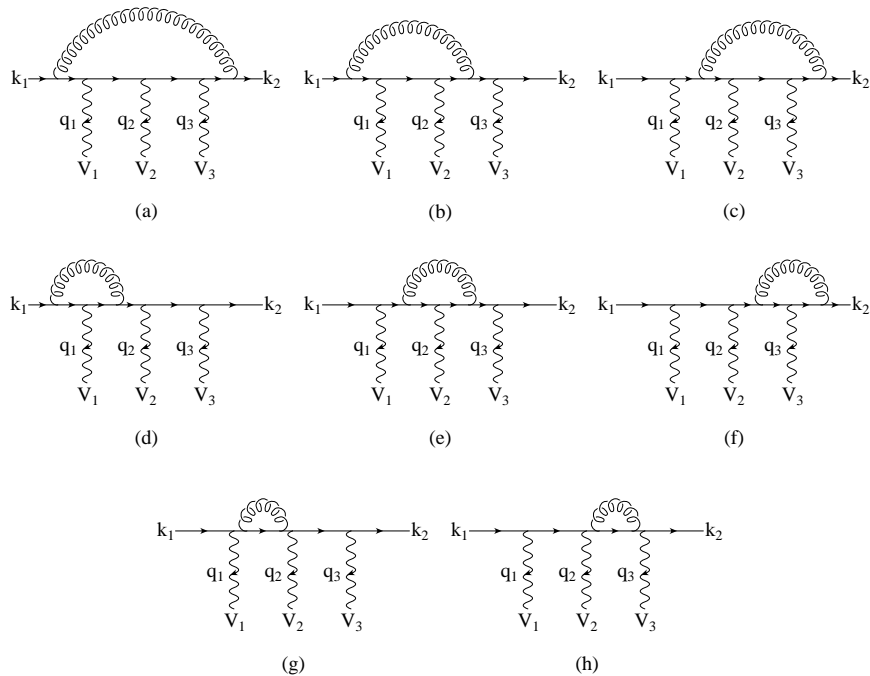
Calculate once, reuse in different processes

Speedup factor  $\approx 70$  compared to MadGraph  
for real emission corrections



# Most challenging for virtual: pentagon corrections

Virtual corrections involve up to pentagons



The sum of all QCD corrections to a single quark line is simple

$$\mathcal{M}_V^{(i)} = \mathcal{M}_B^{(i)} \frac{\alpha_s(\mu_R)}{4\pi} C_F \left( \frac{4\pi\mu_R^2}{Q^2} \right)^\epsilon \Gamma(1 + \epsilon) \left[ -\frac{2}{\epsilon^2} - \frac{3}{\epsilon} + c_{\text{virt}} \right] + \widetilde{\mathcal{M}}_{V_1 V_2 V_3, \tau}^{(i)}(q_1, q_2, q_3) + \mathcal{O}(\epsilon)$$

- Divergent pieces sum to Born amplitude: canceled via Catani Seymour algorithm
- Use amplitude techniques to calculate finite remainder of virtual amplitudes

The external vector bosons correspond to  $V \rightarrow l_1 \bar{l}_2$  decay currents or quark currents

Pentagon tensor reduction with Denner-Dittmaier is stable at 0.1% level

## Phenomenology

Study LHC cross sections within typical VBF cuts

- Identify two or more jets with  $k_T$ -algorithm ( $D = 0.8$ )

$$p_{Tj} \geq 20 \text{ GeV}, \quad |y_j| \leq 4.5$$

- Identify two highest  $p_T$  jets as tagging jets with wide rapidity separation and large dijet invariant mass

$$\Delta y_{jj} = |y_{j_1} - y_{j_2}| > 4, \quad M_{jj} > 600 \text{ GeV}$$

- Charged decay leptons ( $\ell = e, \mu$ ) of  $W$  and/or  $Z$  must satisfy

$$p_{T\ell} \geq 20 \text{ GeV}, \quad |\eta_\ell| \leq 2.5, \quad \Delta R_{j\ell} \geq 0.4, \\ m_{\ell\ell} \geq 15 \text{ GeV}, \quad \Delta R_{\ell\ell} \geq 0.2$$

and leptons must lie between the tagging jets

$$y_{j,\min} < \eta_\ell < y_{j,\max}$$

For scale dependence studies we have considered

$$\mu = \xi m_V \quad \text{fixed scale}$$

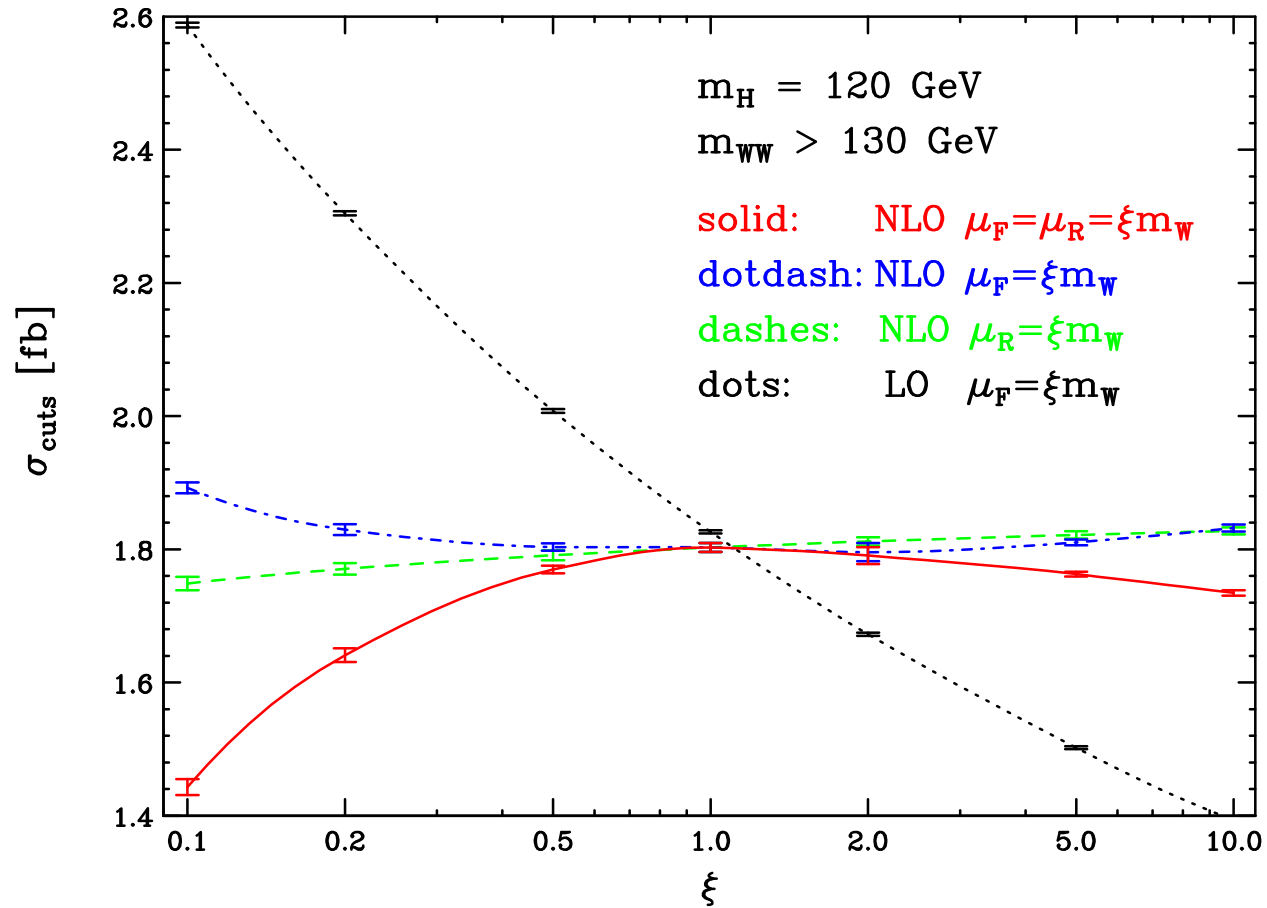
$$\mu = \xi Q_i$$

$$\text{weak boson virtuality : } Q_i^2 = 2k_{q_1} \cdot k_{q_2}$$

# WW production: $pp \rightarrow jje^+ \nu_e \mu^- \bar{\nu}_\mu X$ @ LHC

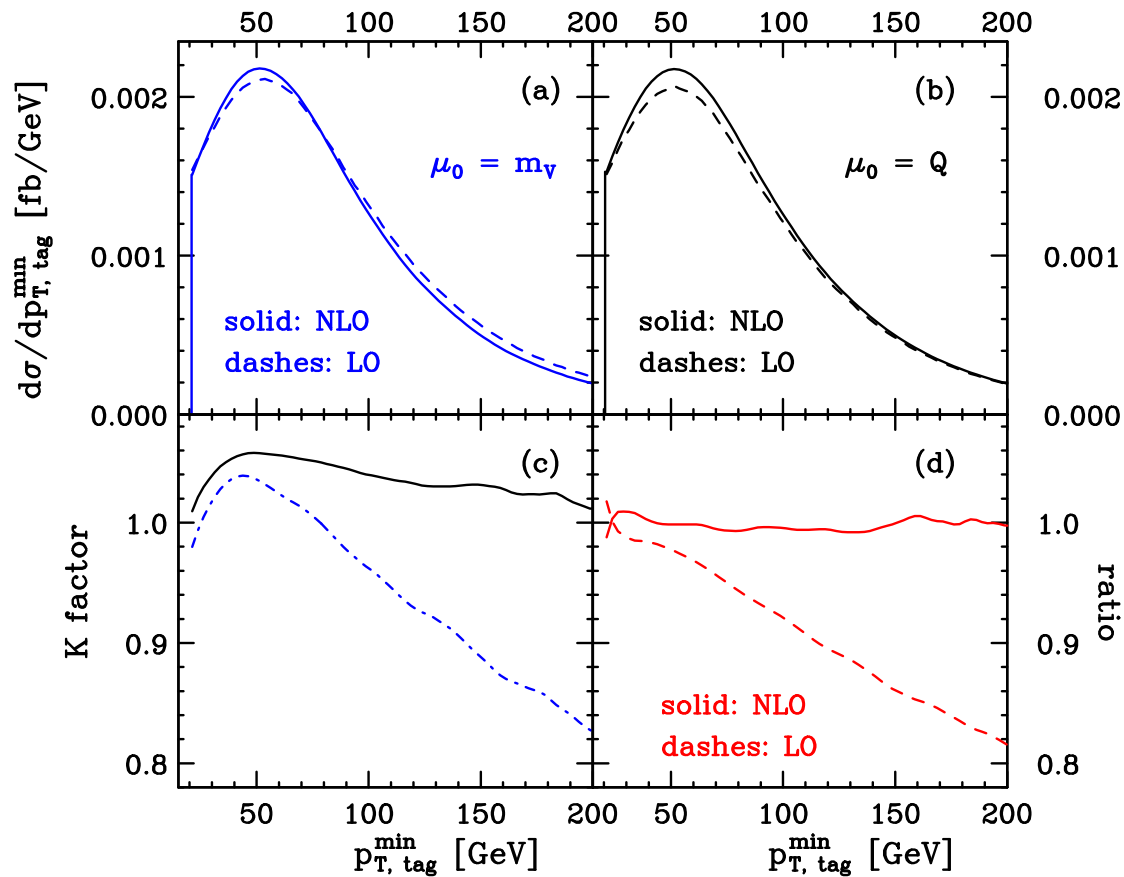
## Stabilization of scale dependence at NLO

Jäger, Oleari, DZ hep-ph/0603177



# WZ production in VBF, $WZ \rightarrow e^+ \nu_e \mu^+ \mu^-$

Transverse momentum distribution of the softer tagging jet



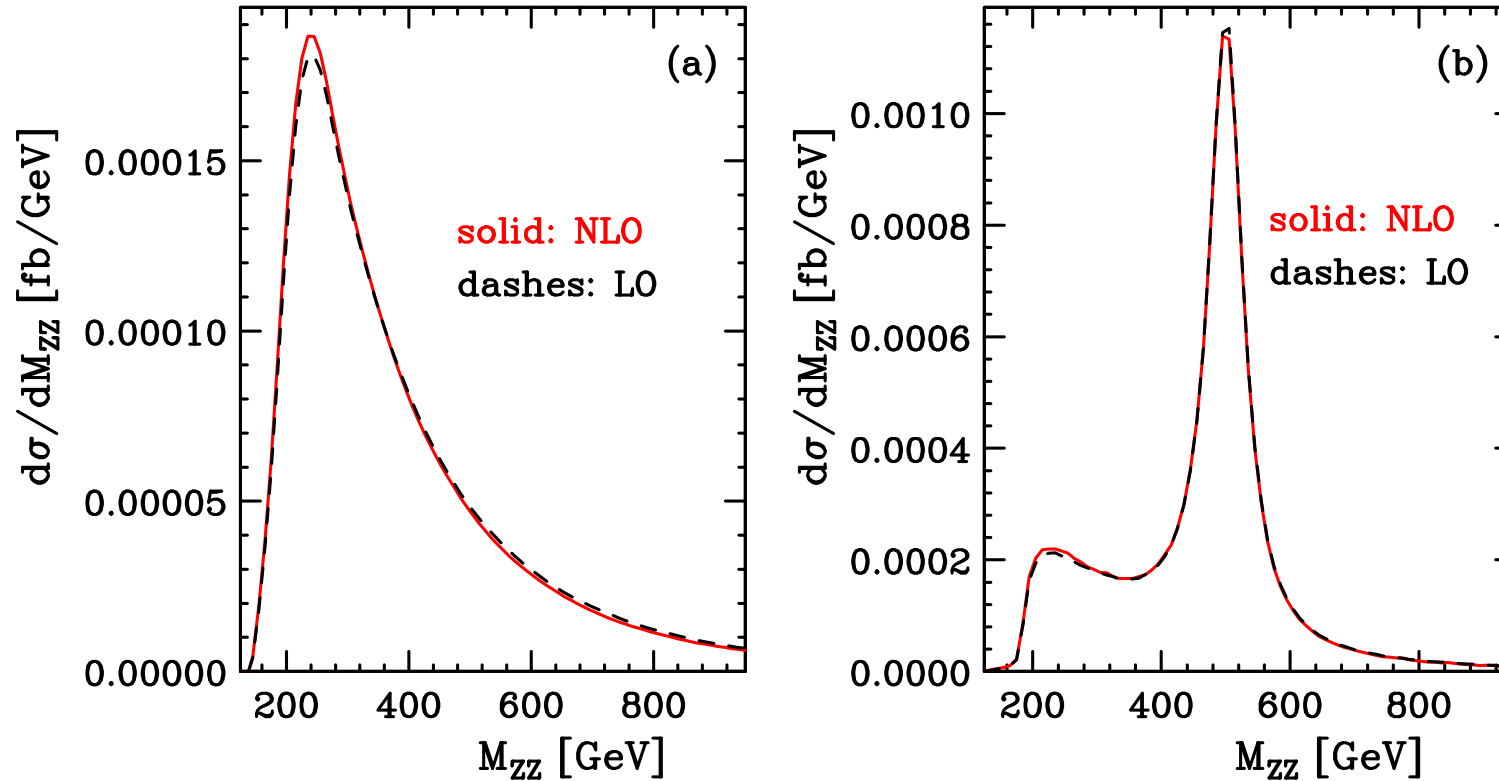
- Shape comparison LO vs. NLO depends on scale
- Scale choice  $\mu = Q$  produces approximately constant  $K$ -factor
- Ratio of NLO curves for different scales is unity to better than 2%: scale choice matters very little at NLO

Use  $\mu_F = Q$  at LO to best approximate the NLO results



## ZZ production in VBF, $ZZ \rightarrow e^+ e^- \mu^+ \mu^-$

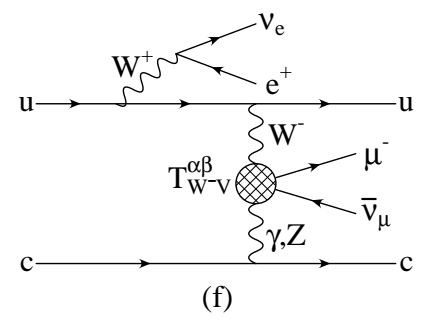
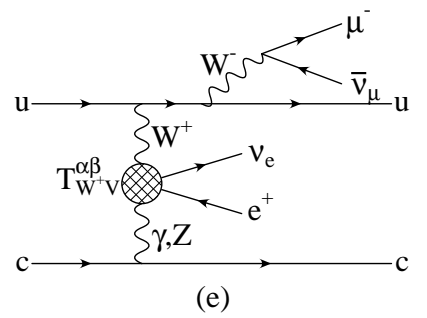
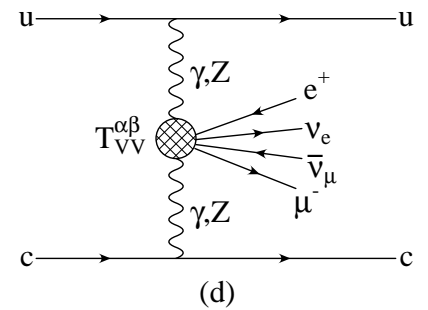
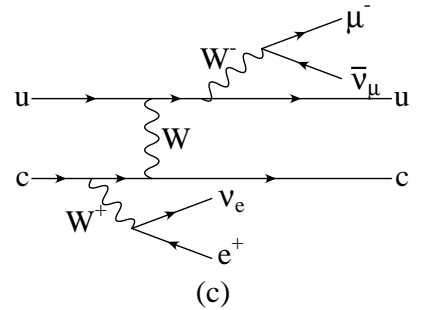
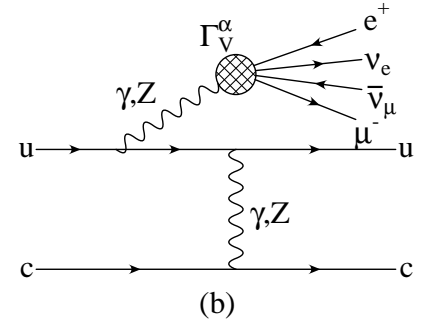
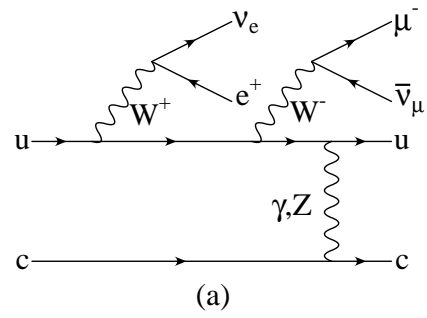
4-lepton invariant mass distribution without/with Higgs resonance



Good agreement of LO and NLO due to low scale choice  $\mu = m_Z$ . Alternative choice  $\mu = m_H$  or  $\mu = m_{4\ell}$  leads to smaller LO cross section at high  $m_{4\ell}$

# $qq \rightarrow qqVV$ : 3 weak bosons on a quark line

- NLO corrections to  $qq \rightarrow qqVV$  contain all loops with a virtual gluon attached to a quark line with one, two or three weak bosons
- Crossing and replacing one quark line by a lepton line yields  $q\bar{q} \rightarrow VVV$  production processes with leptonic decays of the weak bosons
- Recycle virtual contributions from NLO corrections to VBF
- Decompose calculation into modules which can be used in different NLO calculations



## Extending VBFNLO: $VVV$ and $VVj$ Production at NLO QCD

Additional processes implemented in 2008 release of VBFNLO:

- Triple weak boson production:  $VVV = W^\pm W^\mp W^\pm, W^+ W^- Z$  and  $W^\pm ZZ$  with leptonic decay of the weak bosons and full  $H \rightarrow WW$  and  $H \rightarrow ZZ$  contributions  
Work in collaboration with V. Hankele, S. Prestel, C. Oleari and F. Campanario

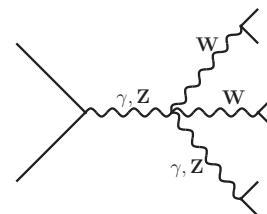
New processes which were made available in 2011 release:

- $W^+ W^- \gamma, ZZ\gamma, WZ\gamma, W\gamma\gamma$  production with leptonic decay of weak bosons  
Work in collaboration with G. Bozzi, F. Campanario, M. Rauch, H. Rzehak
- $W^\pm \gamma j$  and  $WZj$  production (with  $W, Z$  leptonic decay and final state photon radiation)  
Work with C. Englert, F. Campanario, S. Kallweit, M. Spannowsky
- $H\gamma jj$  production in VBF  
Work in collaboration with K. Arnold, B. Jäger, T. Figy
- BSM effects like anomalous couplings and heavy vector resonances

Code is available at <http://www-itp.particle.uni-karlsruhe.de/~vbfnlweb/>

## VVV Production: Motivation

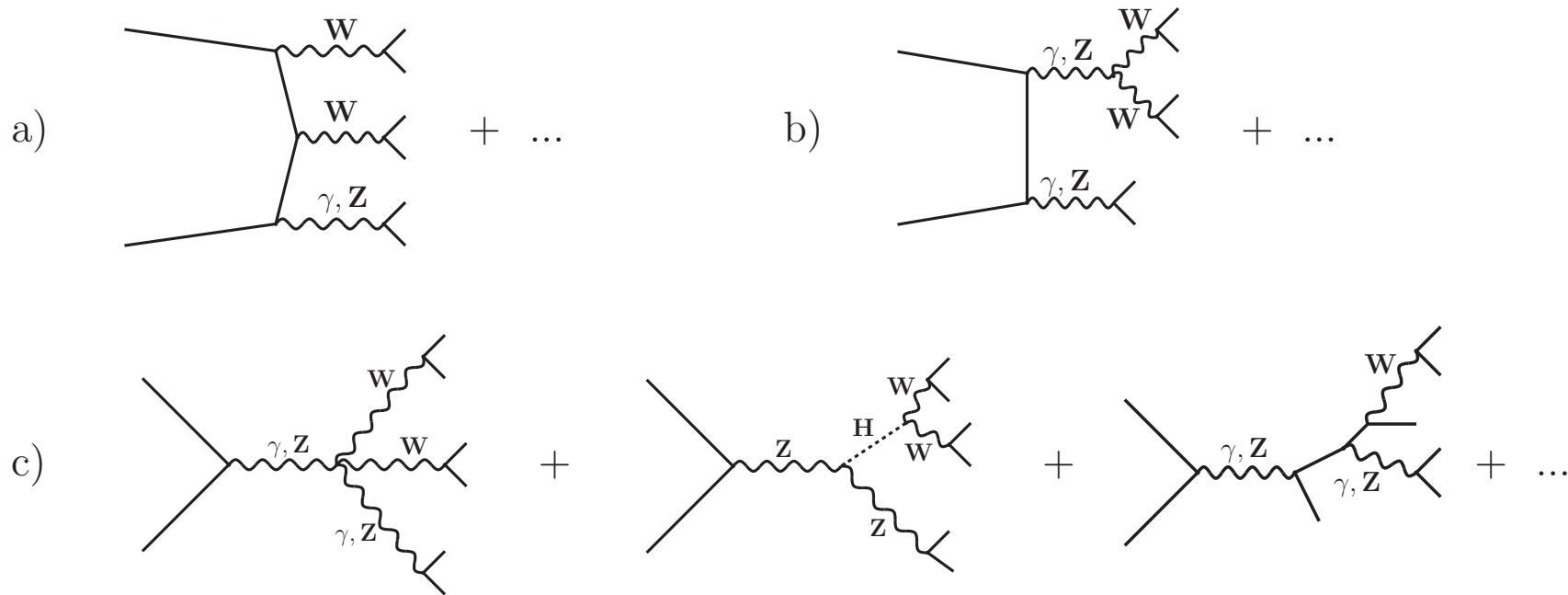
- Standard Model background for SUSY processes with multi-lepton +  $\cancel{p}_T$  signature
- Possibility to obtain information about quartic electroweak couplings.



- QCD corrections to  $pp \rightarrow VVV + X$  on experimentalist's wishlist:  
 [The QCD, EW, and Higgs Working Group: hep-ph/0604120]

process ( $V \in \{Z, W, \gamma\}$ )	relevant for
1. $pp \rightarrow V V \text{ jet}$	$t\bar{t}H$ , new physics
2. $pp \rightarrow t\bar{t} b\bar{b}$	$t\bar{t}H$
3. $pp \rightarrow t\bar{t} + 2 \text{ jets}$	$t\bar{t}H$
4. $pp \rightarrow V V b\bar{b}$	VBF $\rightarrow H \rightarrow VV$ , $t\bar{t}H$ , new physics
5. $pp \rightarrow V V + 2 \text{ jets}$	VBF $\rightarrow H \rightarrow VV$
6. $pp \rightarrow V + 3 \text{ jets}$	various new physics signatures
7. $pp \rightarrow V V V$	SUSY trilepton

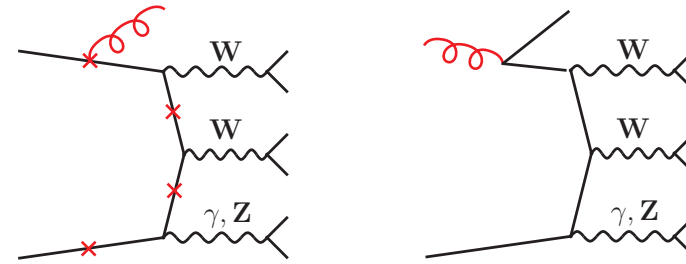
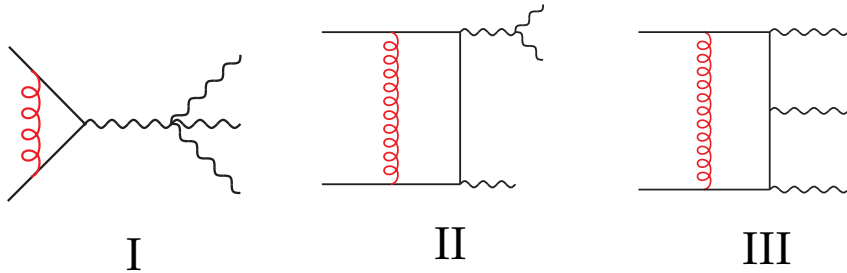
## Example: Contributions to $WWZ$ production



- All resonant and non-resonant matrix elements as well as spin correlations of final state leptons and Higgs contribution included.
- Interference terms due to identical particles in the final state have been neglected.
- All fermion mass effects neglected. ( $H\tau\tau$ -coupling = 0)

# 1-loop matrix elements and real emission matrix elements

Three different topologies:



- I Vertex correction proportional to Born matrix element.
- II Maximally 4-point integrals appear.
- III Up to five external legs (Pentagons):
  - Two independent calculations.
  - Numerically stable results with Denner Dittmaier method.

- Two different classes: final state gluon and initial state gluon.
- Each of them consists of several hundred Feynman-Graphs.
- Soft and collinear singularities subtracted with Catani-Seymour prescription

## Input variables for LHC phenomenology

- PDFs: CTEQ6L1 at LO and CTEQ6M,  $\alpha_S(m_Z) = 0.118$  at NLO.

- Cuts and Masses:

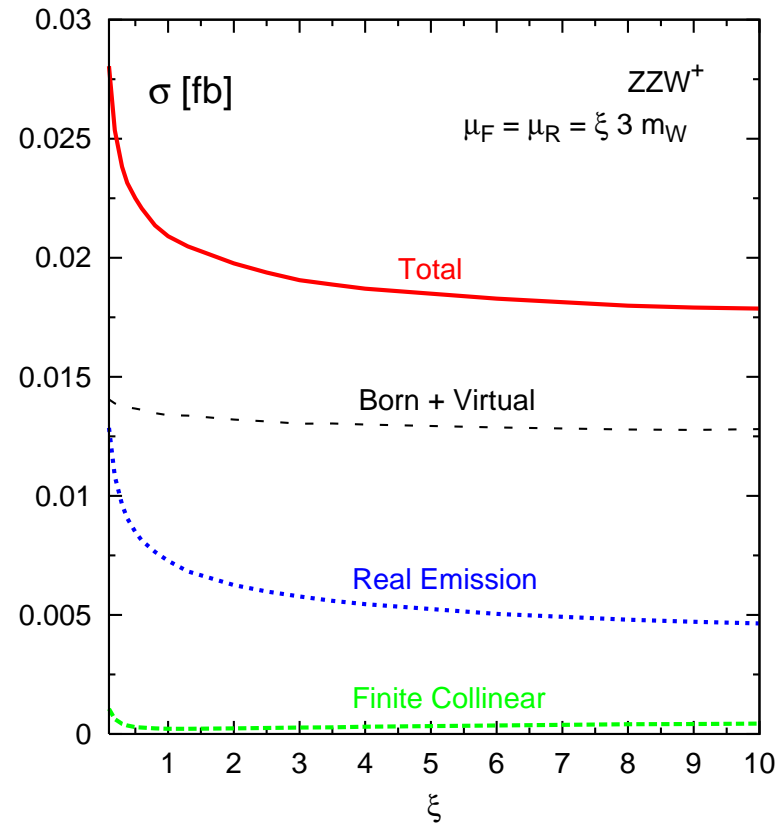
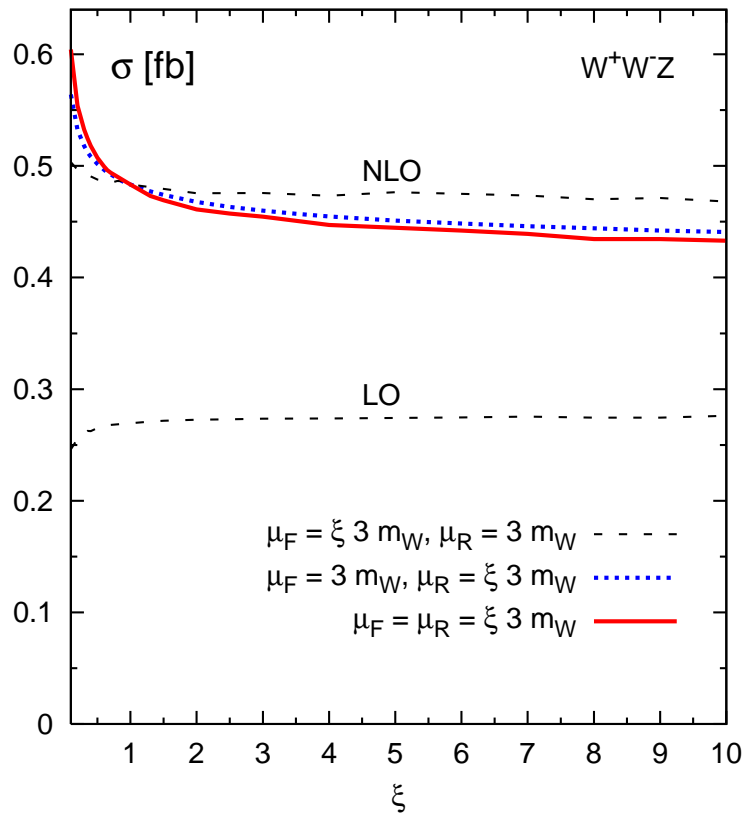
$$p_{T_\ell} > 10 \text{ GeV}, \quad |\eta_\ell| < 2.5, \quad m_{\ell+\ell^-} > 15 \text{ GeV}, \quad m_H = 120 \text{ GeV}.$$

- Renormalization- and Factorization Scale:  $\mu_F = \mu_R = 3 m_W$ .

Following results are for electrons and/or muons in the final state:

⇒ Combinatorial factor of 8/4 for the  $W^+W^-Z/ZZW^\pm$  production compared to three different lepton families in the final state.

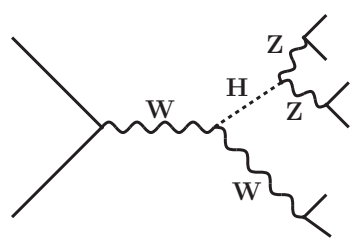
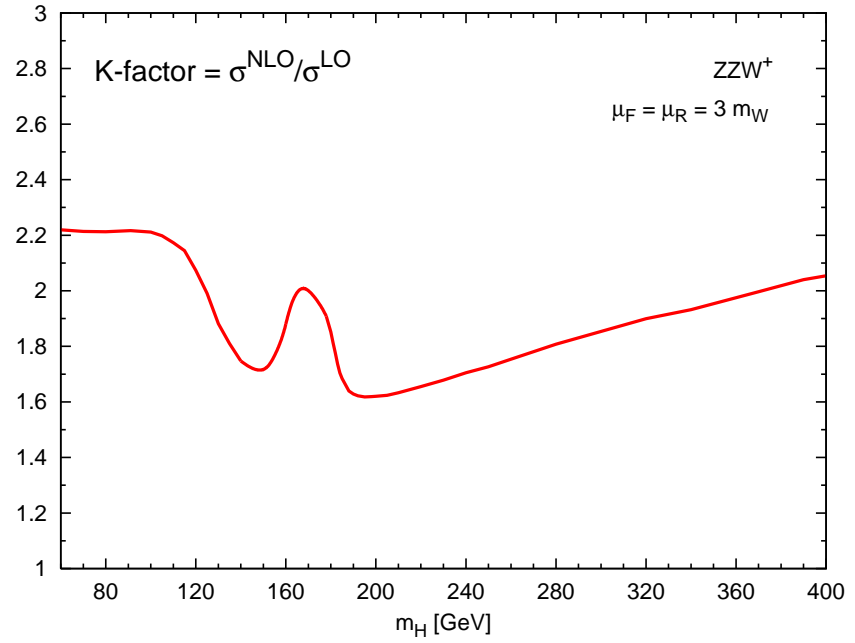
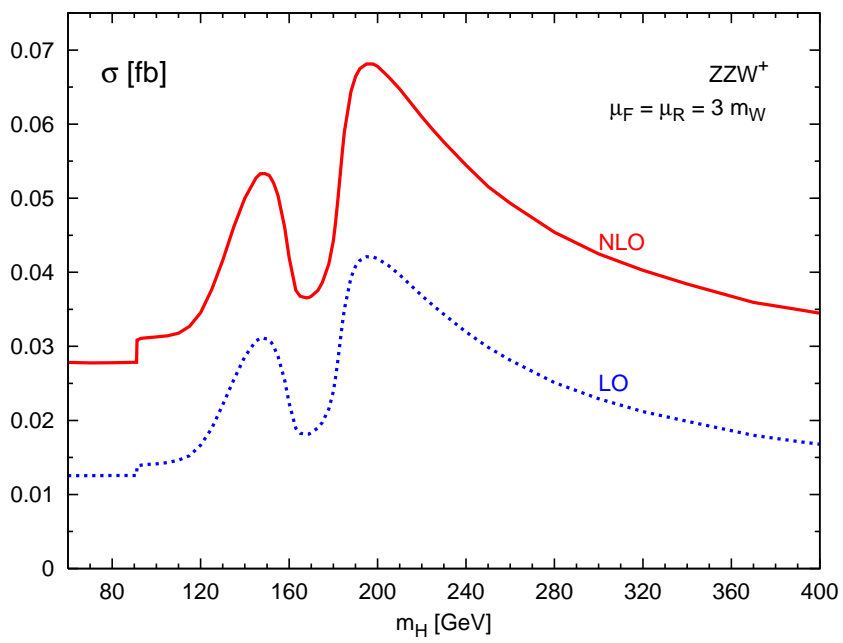
## Scale Dependence



- At LO only small  $\mu_F$ -dependence, no  $\alpha_s(\mu_R)$ .
- At NLO scale dependence is dominated by  $\alpha_s(\mu_R)$ .
- Real emission contribution drives overall scale dependence at NLO.

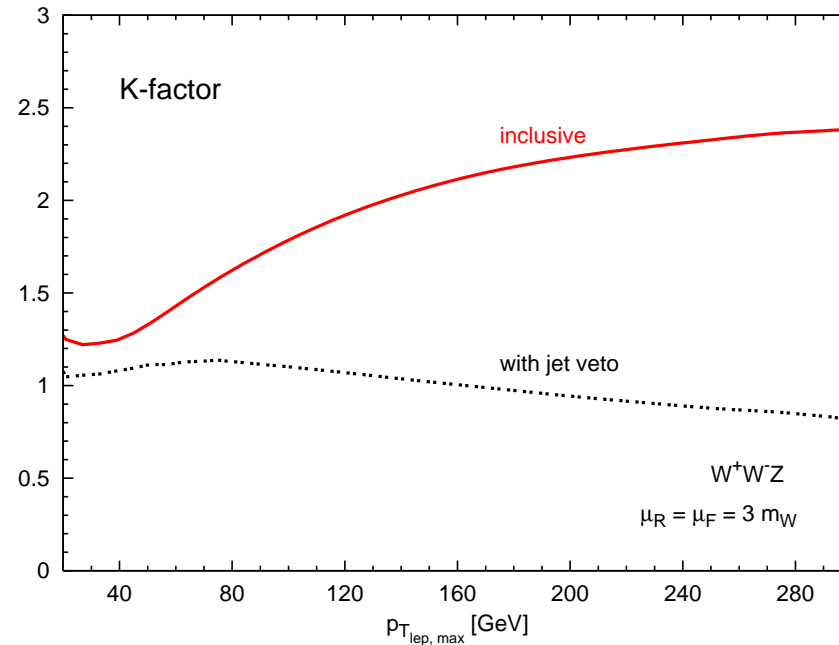
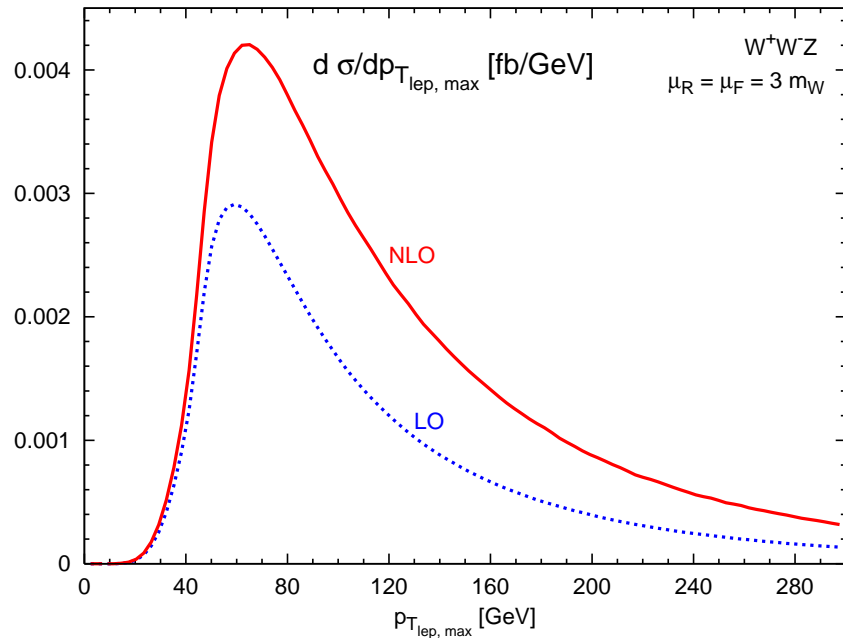


# Higgs mass dependence



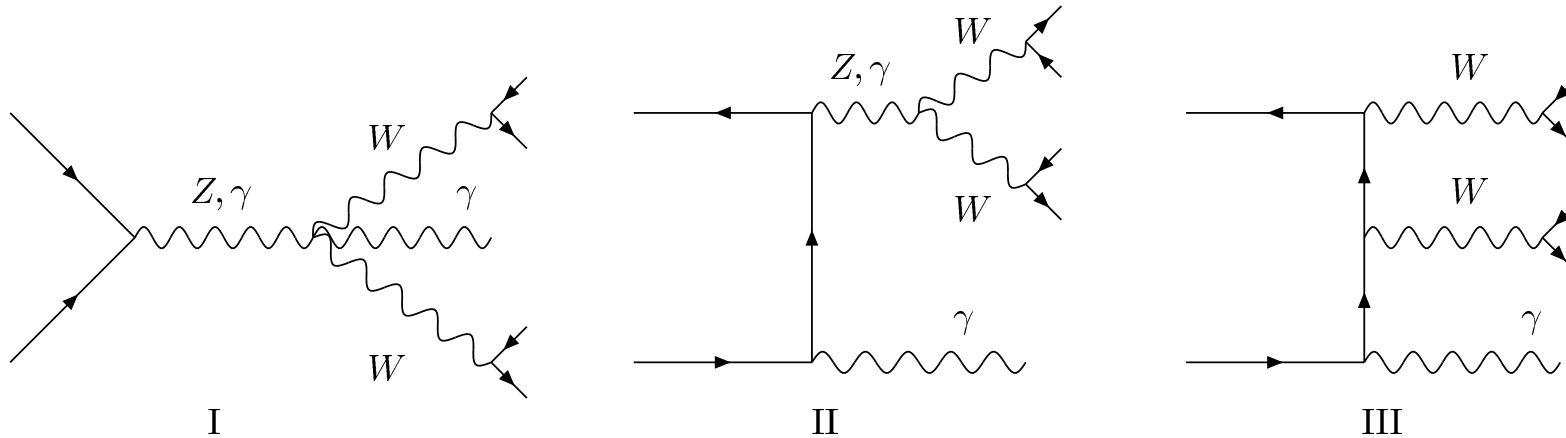
- Cross section reflects behavior of  $BR(H \rightarrow ZZ)$
- K-factor is reduced by Higgs contribution.  
K-factor for  $pp \rightarrow ZH$  production is about  $K = 1.3$   
 $\Rightarrow$  Different  $K$ -factor for resonance production

## Differential cross section and K-factor for the highest- $p_T$ -lepton



- K-factor increases with transverse momentum ( $p_T$ ) by almost a factor of 2.
- Strong phase space dependence due to events with high  $p_T$  jets recoiling against the leptons.
- Veto on jets with  $p_T > 50$  GeV leads to fairly flat K-factor.

## Extension to $W^+W^-\gamma$ and $ZZ\gamma$ Production



New elements of calculation:

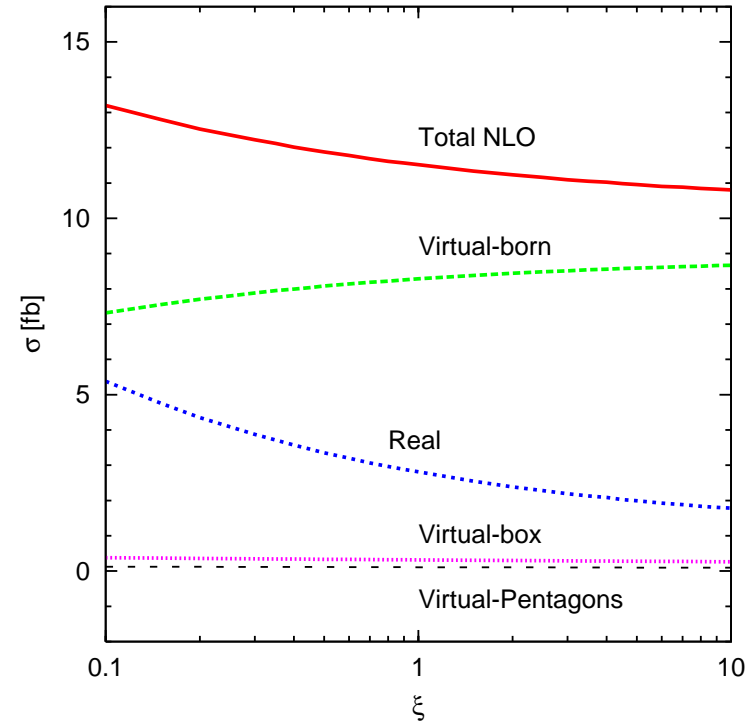
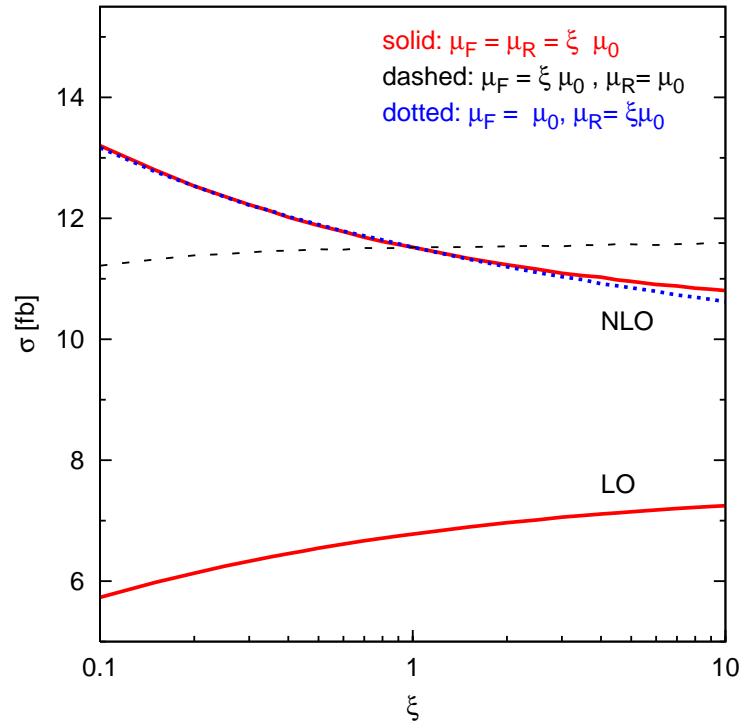
- Different infrared divergence structure of individual loop integrals but same final virtual expressions in terms of finite parts of  $C_{ij}$ ,  $D_{ij}$ , and  $E_{ij}$  functions
- Photon isolation from jets for real emission contributions: use Frixione isolation

$$\sum_i E_{T_i} \theta(\delta - R_{i\gamma}) \leq p_{T_\gamma} \frac{1 - \cos \delta}{1 - \cos \delta_0} \quad (\text{for all } \delta \leq \delta_0)$$

- Final state photon radiation becomes important: adapt phase space to this

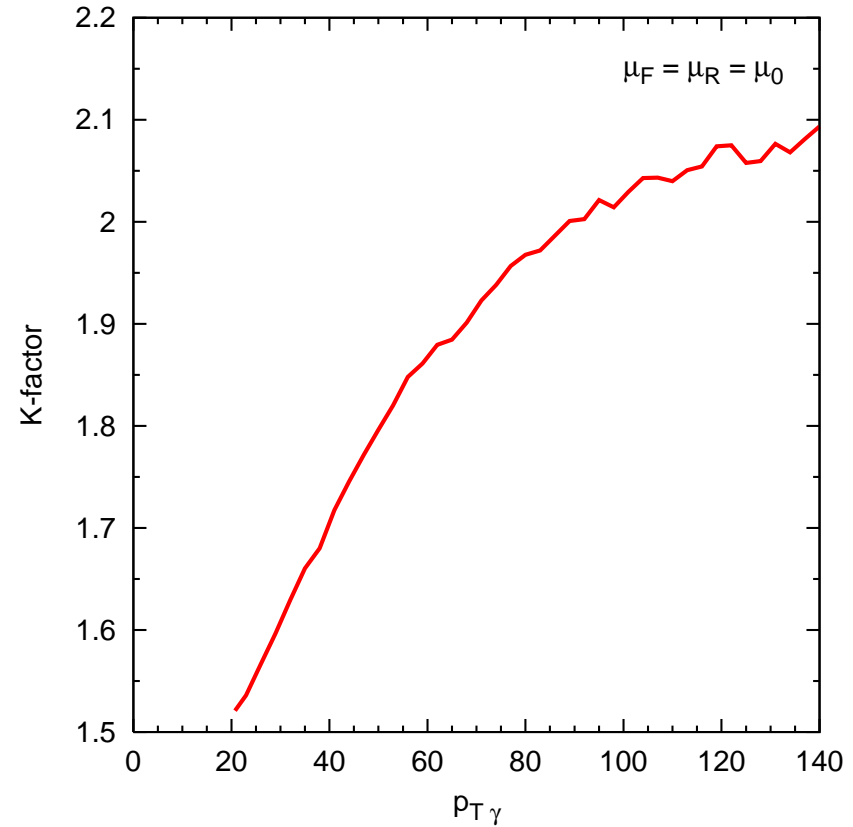
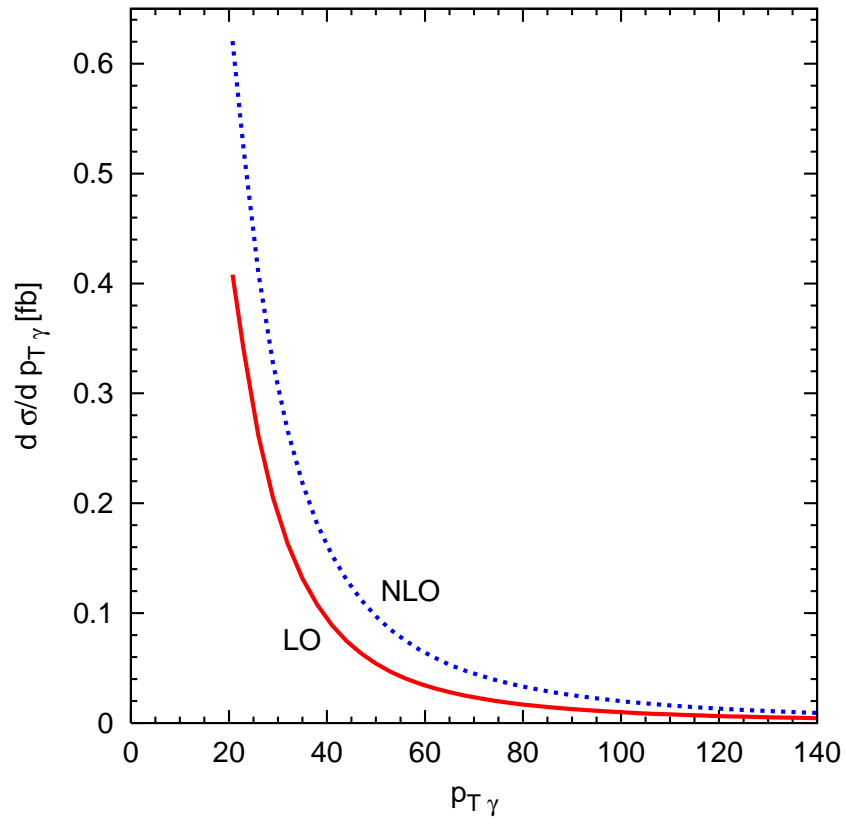
## Scale dependence of integrated cross sections

Variation of  $\mu_F, \mu_R$  about  $\mu_0 = m_{WW\gamma}$



- Behaviour similar to  $VVV$  production: LO scale variation much smaller than NLO correction
- NLO scale dependence largely due to real emission contributions  $\implies$  jet veto will reduce it
- Box and pentagon contributions ( $\tilde{\mathcal{M}}_V$  terms) are quite small: 3% and  $< 1\%$  of total

## NLO Corrections to Distributions: $p_T$ of photon



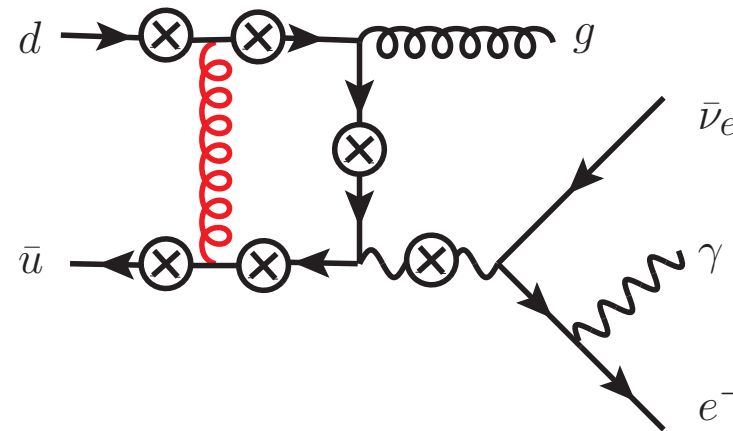
Strong phase space dependence of K-factors (depends on LO scale choice)

## NLO QCD Corrections to $W\gamma j$ Production

- Provide NLO QCD corrections including leptonic  $W$  decay, e.g.

$$pp \rightarrow e^+ \nu_e \gamma j, \quad pp \rightarrow e^- \bar{\nu}_e \gamma j$$

- Sizable cross section at LHC (1.2 pb) and Tevatron (15 fb) for  $p_{Tj}, p_{T\gamma} > 50$  GeV and separation cuts (later)
- Measurement of anomalous  $WW\gamma$  coupling: veto on jets in  $W\gamma$  events requires good knowledge of cross section and distributions: want NLO
- Photon isolation à la Frixione probed at NLO level



- Initial and final state photon radiation. Final radiation from lepton is important
- Virtual corrections up to pentagons
- External gluon already at tree level  $\implies$  *nonabelian* boxes with three gluon vertex
- Larger number of subtraction terms

## Scale dependence: LHC and Tevatron

Identify lepton, photon and one or more jets with  $k_T$ -algorithm ( $D = 0.7$ )

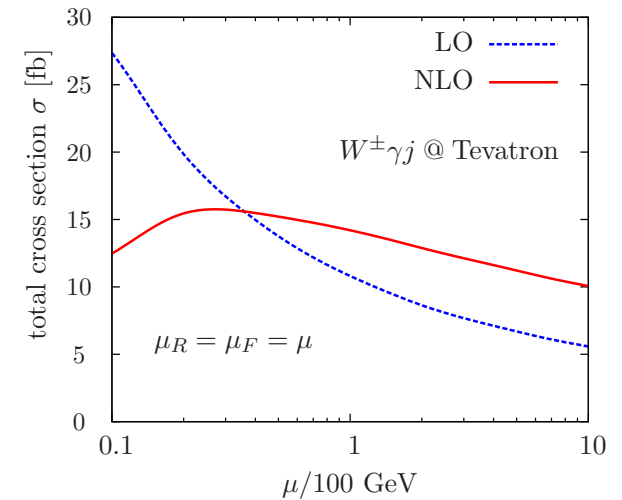
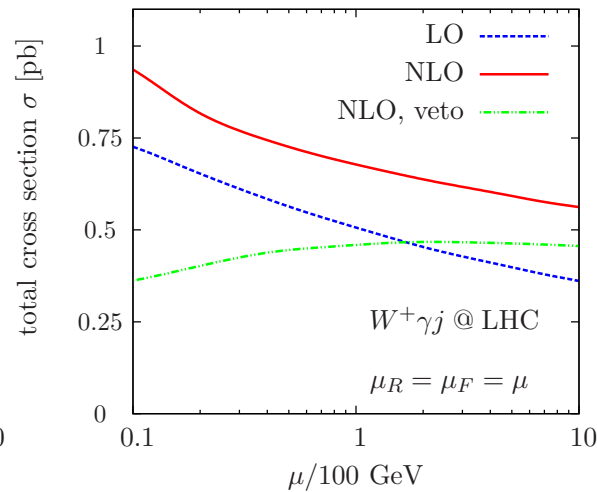
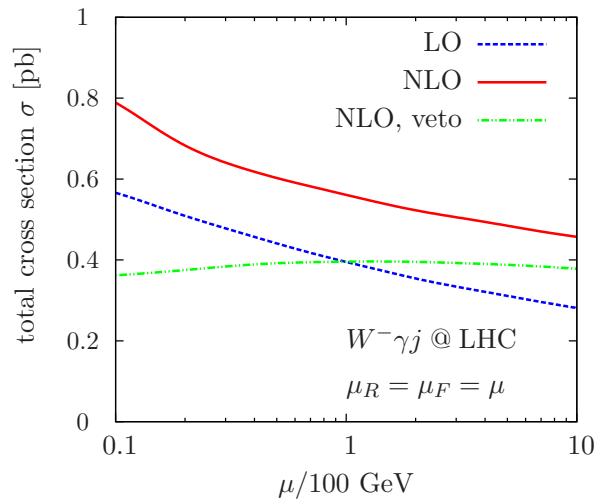
$$p_{Tj,\gamma} \geq 50 \text{ GeV}, \quad |y_j| \leq 4.5, \quad |\eta_\gamma| \leq 2.5,$$

$$p_{Tl} \geq 20 \text{ GeV}, \quad |\eta_l| \leq 2.5$$

$$R_{l,\gamma}, R_{l,j} > 0.2$$

Fraxione isolation of photons with  $\delta_0 = 1$

Cross sections are for  $W \rightarrow e\nu_e$  only

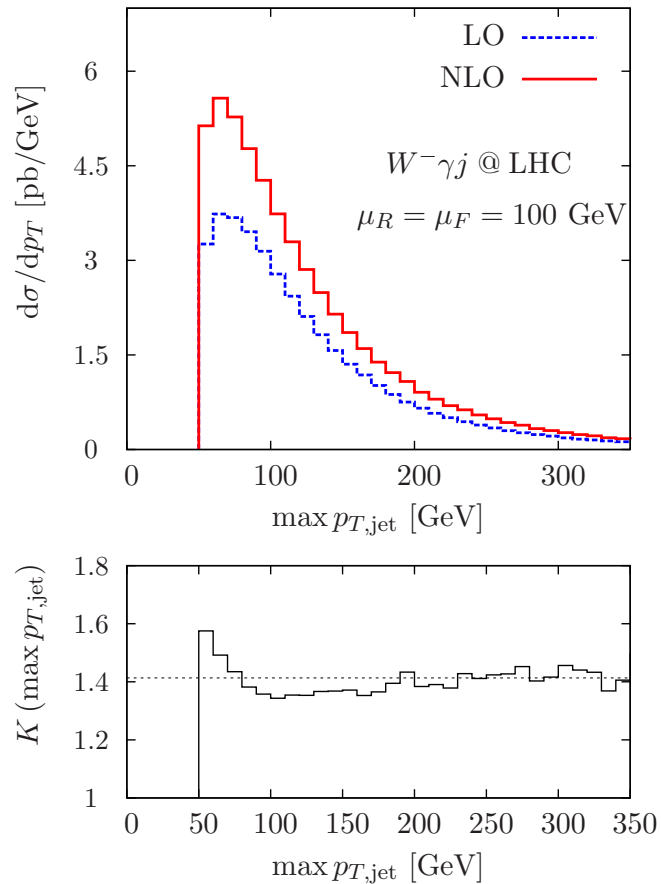


Scale variation at LHC for  $\mu_F = \mu_R = 2^{\pm 1} \cdot 100 \text{ GeV}$ : ±11% at LO reduced to ±7% at NLO

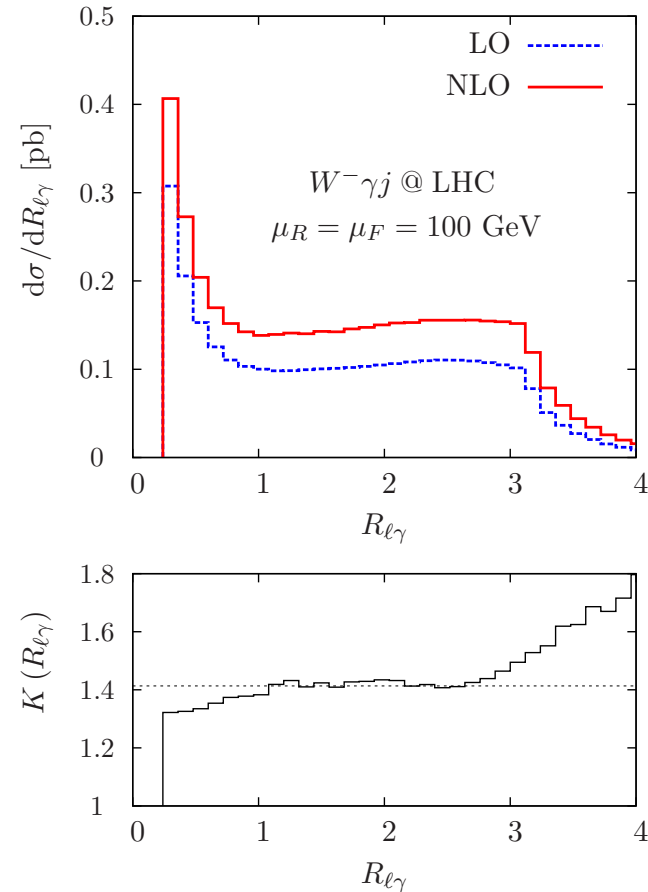
Almost flat behaviour for veto of additional jets of  $p_T > 50 \text{ GeV}$  should be taken as accidental and not as a measure of NLO uncertainties

# NLO corrections to distributions

$p_T$  of hardest jet



lepton photon separation



- Clear shape changes of distributions when going from LO to NLO
- Average K-factor of 1.4 at LHC is significantly larger than LO scale variation



## Conclusions

- VBFNLO provides NLO QCD corrections to a host of processes, in particular vector boson fusion,  $VVV$  production and  $VVj$  production
- All off-shell diagrams as well as the Higgs-contributions have been considered.
- VBFNLO also contains  $hjj$  production from gluon fusion at LO with full quark and squark mass dependence

Code of 2011 release is available at

<http://www-itp.particle.uni-karlsruhe.de/~vbfnlweb>

- Upcoming extensions include  $W\gamma\gamma$  jet production at NLO and  $WZ$  and  $W\gamma$  production with anomalous triple gauge interactions
- VBFNLO is collaborative effort! Thanks to  
V. Hankele, B. Jäger, M. Worek, S. Palmer, F. Campanario, M. Rauch, C. Oleari, K. Arnold, J. Bellm, G. Bozzi, C. Englert, B. Feigl, T. Figy, J. Frank, M. Kerner, G. Klämke, M. Kubocz, S. Plätzer, S. Prestel, H. Rzehak, F. Schissler, M. Spannowsky